Total No. of Questions-8]

Seat

No.

Total No. of Printed Pages—4+1

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## S.E. (Civil) (First Semester) EXAMINATION, 2017 ENGINEERING MATHEMATICS—III (2015 PATTERN)

 Time : Two Hours
 Maximum Marks : 50

 N.B. :- (i)
 Attempt Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6 and Q. No. 7 or Q. No. 8.

- (iii) Neat diagrams must be drawn wherever necessary.
- (iv) Use of electronic pocket calculator is allowed.
- (v) Assume suitable data, if necessary.

(i) 
$$(D^3 - D^2 + 4D - 4)y = e^x$$
.

(*ii*)  $(D^2 + 4)y = \sec 2x$ .

(by method of variation of parameters)

(*iii*) 
$$x^3 \frac{d^3 y}{dx^3} + x^2 \frac{d^2 y}{dx^2} - 2y = \frac{1}{x^3}$$
.

(b) Solve the following equations by using Gauss elimination method : [4]

 $2x_{1} + 4x_{2} + x_{3} = 3$   $3x_{1} + 2x_{2} - 2x_{3} = -2$   $x_{1} - x_{2} + x_{3} = 6$ Or

(a) A light horizontal strut AB of length l is freely pinned at A and B and is under the action of equal and opposite P.T.O.

[8]

compressive forces P at each of its ends and carries a load W at its centre. How that the deflection at its centre is :

where 
$$n^2 = \frac{P}{EI}$$
. [4]

(b) Use Runge-Kutta method of fourth order to obtain y when x = 1.1 for [4]

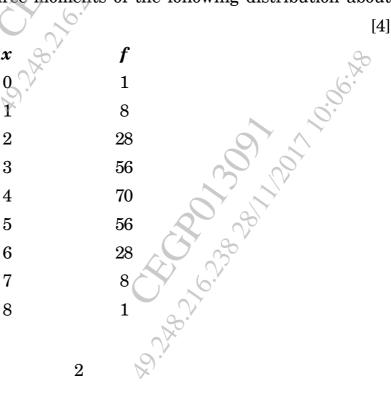
$$\frac{dy}{dx} = x^2 + y^2;$$
  
y(1) = 1.5, h = 0.1

$$4x_{1} + 2x_{2} + 14x_{3} = 14$$
  

$$2x_{1} + 17x_{2} - 5x_{3} = -101$$
  

$$14x_{1} - 5x_{2} + 83x_{3} = 155$$
[4]

**3.** (a) Calculate first three moments of the following distribution about the mean : [4]



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- (b) If mean and variance of a binomial distribution are 12 and 3 respectively, find  $P(r \ge 1)$ . [4]
- (c) Find the directional derivative of  $\phi = x^2 y^2 2z^2$  at the point P(2, -1, 3) in the direction PQ where Q(5, 6, 4).[4] Or
- 4. (a) Prove the following (any one) : [4] (i)  $\nabla . (r^3 \overline{r}) = 3r(r^2 + 1)$ (ii)  $\nabla^2 [\nabla . (r^{-2} \overline{r})] = 2r^{-4}$ (b) Prove that :

$$\overline{\mathbf{F}} = \frac{1}{r} [r^2 \overline{a} + (\overline{a} \cdot \overline{r})\overline{r}]$$

is irrotational.

(c) Obtain correlation coefficient between population density and death rate from the data related to 5 cities. [4]

	Population density	Death rate	
	200	12	0-
	500	18	×
	400	16	
	700		
	300	10	
		Ro Bh	
<b>5.</b> ( <i>a</i> )	Evaluate $\int_{C} \overline{F} \cdot d\overline{r}$ where $\overline{F} = ($	$(x^{2} + y^{2})\hat{i} + (x^{2} - y^{2})\hat{j}$ and C is	the
	curve $y = x^2$ joining $(0, 0)$	and (1, 1).	[5]
[5252]-505	3	P.	.T.O.

[4]

- Using Gauss divergence theorem, for the vector function *(b)*  $\overline{\mathbf{F}} = (x^3 - yz)i - 2x^2y\hat{j} + 2\hat{k}$  evaluate  $\iint_{\overline{\mathbf{F}}} \overline{\mathbf{F}} \cdot d\overline{\mathbf{S}}$ , where S is the surface bounding. The cube x = 0, y = 0, z = 0 and x = a, y = a and z = a. [4]
- Evaluate using Stokes' theorem  $\int_{\overline{F}} \overline{F} d\overline{r}$ , where  $\overline{F} = yz\hat{i} + zx\hat{j} + xy\hat{k}$ (c)and C is the curve  $x^2 + y^2 = 1$ ,  $z = y^2$ . [4]
- Show that  $\overline{F} = (2xy + z^3)\hat{i} + x^2\hat{j} + 3xz^2\hat{k}$  is a conservative force 6. (a)field. Find the work done by the force  $\overline{F}$  in moving the object from (1, -2, 1) to (3, 1, 4). [5]

Evaluate using Stokes theorem  $\iint \nabla \times \overline{\mathbf{F}} \cdot d\overline{\mathbf{S}}$ , where (*b*)

 $\overline{\mathbf{F}} = (2x - y)\hat{i} - yz^2\hat{j} - y^2z\hat{k}$ , where S is the upper half surface of the sphere  $x^2 + y^2 + z^2 = 1$  and  $z \ge 0$ . [4]

Evaluate  $\iint_{S} \overline{r} \cdot \hat{n} \, dS$  over the surface of a sphere of radius 2 (c)with origin as centre. [4]

(a) Solve  $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial r^2}$  subject to the following conditions : 7. [7] $y(0, t) = 0, \forall t$ *(i)* (*ii*)  $y(l, t) = 0, \forall t$ (*iii*)  $\left(\frac{\partial y}{\partial t}\right)_{t=0} = 0$ 

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(*iv*) 
$$y(x, 0) = \frac{3a}{2l}x, 0 < x < \frac{2l}{3}$$
  
=  $\frac{3a}{l}(l-x), \frac{2l}{3} < x < l$ .

An infinitely long plane uniform plate is bounded by two parallel (*b*) edges in the y-direction and an end at right angles to them. The breadth of the plate is  $\pi$ . This end is maintained at the constant temperature 40°C at all points and other edges at zero temperature. Find the steady state temperature u(x, y).[6] Or

Solve  $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$  subject to the following conditions : (i) u is finite for all t(ii)  $u(0, t) = 0, \forall t$ (iii)  $u(l, t) = 0, \forall t$ (iii)  $u(l, t) = 0, \forall t$ *(a)* 8. [7]

(iv) 
$$u(x, 0) = \pi x - x^2, 0 \le x \le \pi$$
.

Solve the wave equation : (*b*)

$$\frac{\partial^2 u}{\partial t^2} = a^2 \frac{\partial^2 u}{\partial x^2}$$

[6]

 $\begin{aligned} \int t & f \\ (ui) & \left(\frac{\partial u}{\partial t}\right)_{t=0} = 0 \\ (iv) & u(x, 0) = 2x, 0 < x < \pi. \end{aligned}$ 

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