

Total No. of Questions : 10]

SEAT No. :

P3130

[Total No. of Pages : 3

[5354]-620

B.E. (E & TC)

DETECTION AND ESTIMATION THEORY

(2012 Pattern) (Elective - IV)

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) Attempt Q.No. 1 or Q.2, Q.3 or Q.4, Q.5 or Q.6, Q7 or Q.8, Q.9 or Q.10.
- 2) Figures to the right indicate full marks.

Q1) a) Write characteristics of Maximum Likelihood Estimator. [5]

b) What is Bayes criteria. Derive the expression for Bayes Decision rule. Under what condition Bayes criteria reduces to LRT and MAP. [5]

OR

Q2) a) Explain Recursive Least Square Estimation. [5]

b) Explain how decision rule is framed in case of multiple hypothesis tests.[5]

Q3) a) Write a short note on Minimum Variance Unbiased Estimator. [5]

b) State and explain Cramer-Rao inequality for a Random Parameter. [5]

OR

Q4) a) A ternary communication system transmits one of the three amplitude signal {1, 2, 3} with equal probabilities. The independent received signal samples under each hypothesis are [5]

$$H1 : Y_k = 1 + N \quad K = 1, 2..K$$

$$H2 : Y_k = 2 + N \quad K = 1, 2...K$$

$$H3 : Y_k = 3 + N \quad K = 1,2,...K$$

The additive noise N is Gaussian with mean zero and variance σ^2 . The costs are $C_{ii} = 0$ and $C_{ij} = 1$ for $i \neq j$. $I_j, j = 1, 2, 3$ determine the decision regions

P.T.O.

- b) Discuss the Bayes estimation method briefly for Least Square Estimation and Kalman filter. [5]

Q5) a) Write a note on Discrete Wiener Filter. [8]

- b) Explain Kalmans filter in context of estimation theory. [8]

OR

Q6) a) What is Cramer Rao Bound inequality and what are its limitations discuss in detail. [8]

- b) Write a note on Recursive Least-Square Estimator. [8]

Q7) a) In the received signal under hypothesis H_1 and H_0 was [8]

$$H_1 : Y_k = m + N_k, \quad k = 1, 2, \dots, K$$

$$H_0 : Y_k = N_k, \quad k = 1, 2, \dots, K$$

- i) Assuming the constant m is unknown. Obtain the Maximum Likelihood estimation of the mean
- ii) Suppose now mean ' m ' is known but the variance is unknown. Obtain the MLE.
- b) In on-off keying system, the source transmits signal of amplitude I volt or 0 volt. Noise $n(t)$ is added which has zero mean and variance = 1 and it is Gaussian. Set up the LRT (Likelihood Ratio Test) for this problem. [8]

OR

Q8) a) A rectangular pulse of known amplitude A is transmitted starting at time instant t_0 with probability $1/2$. The duration T of the pulse is a random variable uniformly distributed over the interval $[T_1, T_2]$. The additive noise to the pulse is white Gaussian with mean zero and variance $N_0/2$. Determine the likelihood ratio. [8]

- b) Explain best linear unbiased Estimator (BLUE)? [8]

- Q9)** a) Explain the Radar Elementary concepts- Range, Range Resolution, and Doppler Shift. [9]
- b) Give a Review of Some CFAR Detectors. [9]

OR

- Q10)**a) What is CFAR Detection and state the Principles of Adaptive CFAR Detection. [9]
- b) Write short note on Neyman-Pearson detector. [9]

